

This listing of claims will replace all prior versions, and listings, of claims in the application.

**Listing of Claims:**

1. (Currently Amended) A system for searching web pages comprising:  
  
a database for storing connectivity information about the web pages; and  
  
a page-grading engine associated with an approximation matrix  $Q'$ , where  $Q'$  approximates an ideal matrix  $Q$  with respect to the connectivity information; wherein the page-grading engine receives as input a personalization description  $v$  describing a set of preferences among the web pages, and grades search results with respect to  $Q'$  and  $v$ , wherein non-zero entries of a vector indicative of the personalization description  $v$  correspond at least to a favorites list associated with a user's web browser.
2. (Original) The system of claim 1 wherein approximation matrix  $Q'$  is a rank- $k$  matrix whose representation comprises a singular value decomposition comprising matrices  $V_k$ ,  $S$  and  $U_k^T$  for a parameter  $k$ .
3. (Original) The system of claim 2 wherein  $v$  is a vector and  $Q'$  times  $v$  is an optimal approximation to  $Q$  times  $v$  over all rank- $k$  matrices.
4. (Currently Amended) A method of grading objects from an interconnected collection of weighted objects, the weights of the objects described by a description  $v$ , and the interconnection of the objects described by a description  $P$ , the method comprising:  
  
applying a grading function  $Q'$  to the description  $v$  for the objects to determine a set of grades for the objects; ~~and~~  
  
assigning at least one object the corresponding determined grade for that object; wherein the grading function  $Q'$  approximates an ideal grading function  $Q$ , wherein non-zero entries of a vector indicative of the personalization description  $v$  correspond

at least to a favorites list associated with a user's web browser and wherein ~~where~~  
applying ideal grading function  $Q$  to the description  $v$  produces ideal grades with  
respect to description  $P$  for every object in the interconnected collection of weighted  
objects; and  
rendering an indication of at least one graded object.

5. (Original) The method of claim 4 wherein  $P$ ,  $Q$ , and  $Q'$  are matrices,  $v$  is a vector, and the approximation is a low-rank optimal approximation.

6. (Previously Presented) The method of claim 5 wherein entry  $P[i,j]$  in matrix  $P$  represents the probability of reaching one object  $i$  from another object  $j$  in one step of a random walk among the weighted objects.

7. (Original) The method of claim 6 wherein at each step of the random walk there is a fixed probability  $c$  that the walk will reset, and that the random walk then continues from object  $a$  with probability  $v[a]$ .

8. (Original) The method of claim 7 wherein the ideal grade of an object  $b$  is the probability of arriving at object  $b$  at a step of the random walk.

9. (Original) The method of claim 5 wherein the objects are web pages.

10. (Currently Amended) A method of grading objects from an interconnected collection of weighted objects by approximating a matrix  $Q$  with respect to a parameter  $k$ , comprising:

computing a matrix  $U_k$ ;

computing a matrix  $V_k$ ;

computing a diagonal matrix  $S$ ;  
defining the approximation to  $Q$  as the matrix product  $V_k S U_k^T$ ; and  
determining a grade for at least one of the objects using the approximation to  $Q$ ;  
wherein the weights of the objects are described by a vector  $v$ , wherein non-zero entries of the vector  $v$  correspond at least to a favorites list associated with a user's web browser, the interconnection of the objects is described by a matrix  $P$ , and the ideal grade of object  $i$  with respect to matrix  $P$  equals  $Q[i]$  times  $v$  where  $Q[i]$  is the  $i$ th row of an ideal matrix  $Q$ .

11. (Original) The method of claim 10 further comprising:  
choosing a sufficiently large parameter  $d$ ; and  
computing an intermediate matrix  $M$  with respect to  $P$ ; wherein matrix  $U_k$ , comprises the  $k$  principal eigenvectors of  $dI - MM^T$  and matrix  $V_k$  comprises the  $k$  principal eigenvectors of  $dI - M^T M$ , and wherein matrix  $S = (dI - D)^{-1/2}$ , where  $D$  is the diagonal matrix comprising the  $k$  eigenvalues corresponding to the  $k$  principal eigenvectors of  $dI - MM^T$ .
12. (Original) The method of claim 11 wherein computing an intermediate matrix  $M$  with respect to  $P$  is further with respect to a constant  $c$ .
13. (Currently Amended) A system for grading objects from an interconnected collection of weighted objects comprising:  
a description  $v$  of the weights of the objects, wherein non-zero entries of a vector indicative of the description  $v$  correspond at least to a favorites list associated with a user's web browser;  
a description  $P$  of the interconnection of the objects; and

a processor comprising an object-grading engine for approximating an ideal grading function  $Q$  with an approximate function  $Q'$ , where applying ideal grading function  $Q$  to the description  $v$  produces ideal grades with respect to description  $P$  for every object in the interconnected collection of weighted objects, and for assigning at least one object the grade produced for that object by an application of  $Q'$  to  $v$ .

14. (Original) The system of claim 13 further comprising a search engine in connection with the object-grading engine, wherein the object-grading engine grades objects passed from the search engine.

15. (Original) The system of claim 13 wherein the objects are web pages.

16. (Currently Amended) A computer-readable storage medium including computer-executable instructions facilitating the grading of web pages, the web pages interconnected corresponding to a matrix  $P$ , computer-executable instructions executing the steps of:

computing a representation of an approximation matrix  $Q'$  to an ideal matrix  $Q$ ; and  
applying  $Q'$  to a personalization vector  $v$  to obtain grades of the web pages, wherein non-zero entries of the vector  $v$  correspond at least to a favorites list associated with a user's web browser.

17. (Original) The computer-readable medium of claim 16 wherein  $Q'$  is a rank- $k$  matrix whose representation comprises a singular value decomposition comprising matrices  $V_k$ ,  $S$  and  $U_k^T$  for a parameter  $k$ .

18. (Original) The computer-readable medium of claim 17 wherein  $Q'$  times  $v$  is an optimal approximation to  $Q$  times  $v$  over all rank- $k$  matrices.

19. (Original) The computer-readable medium of claim 17, the computer-executable instructions further executing the steps of:

applying the grading of web pages produced by Q' to the results of a search query;  
and  
outputting the results of the search query sorted according the grading.